Roll No: $\square$

## B. TECH. <br> (SEM-V) THEORY EXAMINATION 2020-21 DESIGN AND ANALYSIS OF ALGORITHM

Time: 3 Hours
Total Marks: 100
Note: 1. Attempt all Sections. If require any missing data; then choose suitably.
SECTION A

1. Attempt all questions in brief.
$2 \times 10=20$

| Qno. | Question | Marks | CO |
| :--- | :--- | :--- | :--- |
| a. | What is recurrence relation? How is a recurrence solved using master's <br> theorem? | 2 |  |
| b. | What is asymptotic notation? Explain Omega $(\Omega)$ notation? | 2 |  |
| c. | Write down the properties of binomial tree. | 2 |  |
| d. | Differentiate Backtracking algorithm with branch and bound algorithm. | 2 |  |
| e. | Solve the recurrence T (n) $=\mathbf{4 T ( n / 2 ) + \mathbf { n } ^ { 2 }}$ | 2 |  |
| f. | Explain Fast Fourier Transform in brief. | 2 |  |
| g. | Write an algorithm for naive string matcher? | 2 |  |
| h. | Explain searching technique using divide and conquer approach. | 2 |  |
| i. | Explain Skip list in brief. | 2 |  |
| j. | Explain how algorithms performance is analyzed? | 2 |  |

## SECTION B

## 2. Attempt any three of the following:

| Qno. | Question | Marks | CO |
| :---: | :---: | :---: | :---: |
| a. | Write an algorithm for counting sort? Illustrate the operation of counting sort on the following array: $\mathbf{A}=\{\mathbf{4}, \mathbf{0}, \mathbf{2}, \mathbf{0}, \mathbf{1}, \mathbf{3}, \mathbf{5}, \mathbf{4}, \mathbf{1 , 3}, \mathbf{2}, \mathbf{3}\}$ | $10$ |  |
| b. | Show the results of inserting the keys F, S, Q, K, C, L, H, T, V, W, M, R, N, P, A, B, X, Y, D, Z, E in order into an empty B-tree. Use $t=3$, where $t$ is the minimum degree of $B$ - tree. | 10 |  |
| c. | Discuss greedy approach to an activity selection problem of scheduling several competing activities. Solve following activity selection problem $\begin{aligned} & \mathrm{S}=\{\mathrm{A} 1, \mathrm{~A} 2, \mathrm{~A} 3, \mathrm{~A} 4, \mathrm{~A} 5, \mathrm{~A} 6, \mathrm{~A} 7, \mathrm{~A} 8, \mathrm{~A} 9, \mathrm{~A} 10\} \\ & \mathrm{S}_{\mathrm{i}}=\{1,2,3,4,7,8,9,9,11,12\} \mathrm{F}_{\mathrm{i}}=\{3,5,4,7,10,9,11,13,12,14\} \end{aligned}$ | 10 |  |
| d. | What is sum of subset problem? Draw a state space tree for Sum of subset problem using backtracking? Let $\mathbf{n}=\mathbf{6}, \mathbf{m}=\mathbf{3 0}$ and $\mathbf{w}[\mathbf{1 : 6}]=\{\mathbf{5}, \mathbf{1 0}$, $12,13,15,18\}$ | 10 |  |
| e. | Write KMP algorithm for string matching? Perform the KMP algorithm to search the occurrences of the pattern abaab in the text string abbabaabaabab. | 10 |  |

## SECTION C

## 3. Attempt any one part of the following:

| Qno. | Question | Marks | CO |
| :--- | :--- | :--- | :--- |
| a. | Solve the following recurrence relation: <br> i. $\mathbf{T}(\mathbf{n})=\mathbf{T}(\mathbf{n}-\mathbf{1})+\mathbf{n}^{4}$ <br> ii. $\mathbf{T}(\mathbf{n})=\mathbf{T}(\mathbf{n} / \mathbf{4})+\mathbf{T}(\mathbf{n} / \mathbf{2})+\mathbf{n}^{2}$ | 10 |  |
| b. | Write an algorithm for insertion sort. Find the time complexity of <br> Insertion sort in all cases. | 10 |  |

Roll No: $\square$
4. Attempt any one part of the following:

| Qno. | Question | Marks | CO |
| :--- | :--- | :--- | :--- |
| a. | Write an algorithm for insertion of key in the Red-Black Tree. Discuss <br> the various cases for insertion of key in red-black tree for given sequence <br> of key in an empty red-black tree- $\mathbf{5 , 1 6 , \mathbf { 2 2 , 2 5 } , \mathbf { 2 , 1 0 , 1 8 , 3 0 , 5 0 , 1 2 , 1 . }}$ | 10 |  |
| b. | Explain and write an algorithm for union of two binomial heaps and also <br> write its time complexity? | 10 |  |

## 5. Attempt any one part of the following:

| Qno. | Question | Marks | CO |
| :--- | :--- | :--- | :--- | :--- |
| a. | Define minimum spanning tree (MST). Write Prim's algorithm to <br> generate a MST for any given weighted graph. Generate MST for the <br> following graph using Prim's algorithm. | 10 |  |
| b. | Explain Dijkstra's algorithm to solve single source shortest path problem <br> with suitable example. | 10 |  |

6. Attempt any one part of the following:


## 7. Attempt any one part of the following:

| Qno. | Question | Marks | CO |
| :--- | :--- | :--- | :--- |
| a. | Write short notes on following: <br> (i.) $\quad$ Randomized algorithm. <br> (ii.) NP- complete and NP hard. | 10 |  |
| b. | What is approximation algorithm? Explain set cover problem using <br> approximation algorithm. | 10 |  |

