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Sub Code: RAS203										
Roll No.										

B. TECH (SEM-II) THEORY EXAMINATION 2017-18 ENGINEERING MATHEMATICS - II

Time: 3 Hours

Total Marks: 70

 $2 \ge 7 = 14$

 $7 \ge 3 = 21$

7 x 1 = 7

Note: Attempt all Sections. If require any missing data, then choose suitably.

SECTION A

1. Attempt *all* questions in brief.

- (a) Determine the differential equation whose set of independent solutions is $\{e^x, xe^x, x^2e^x\}$.
- **(b)** Solve: $(D+1)^3 y = 2e^{-x}$.
- (c) Prove that: $P_n(-x) = (-1)^n P_n(x)$.
- (d) Find inverse Laplace transform of $\frac{s+8}{s^2+4s+5}$.
- (e) If $L\left\{F(\sqrt{t})\right\} = \frac{e^{-1/s}}{s}$, find $L\left\{e^{-t}F(3\sqrt{t})\right\}$.

(f) Solve:
$$(D+4D'+5)^2 z = 0$$
, where $D \equiv \frac{\partial}{\partial x}$, $D' \equiv \frac{\partial}{\partial y}$.

(g) Classify the equation:
$$z_{xx} + 2x z_{xy} + (1 - y^2) z_{yy} = 0$$
.

SECTION B

2. Attempt any *three* of the following:

(a) Solve
$$(D^2 - 2D + 4)y = e^x \cos x + \sin x \cos 3x$$
.

(b) Prove that:
$$J_{5/2}(x) = \sqrt{\frac{2}{\pi x}} \left[\left(\frac{3 - x^2}{x^2} \right) \sin x - \frac{3 \cos x}{x} \right]$$

(c) Draw the graph and find the Laplace transform of the triangular wave function of period 2π given by

$$F(t) = \begin{cases} t, & 0 < t \le \pi \\ 2\pi - t, & \pi < t < 2\pi \end{cases}$$

(d) Obtain half range cosine series for
$$e^x$$
 the function $f(t) = \begin{cases} 2t, & 0 < t < 1\\ 2(2-t), 1 < t < 2 \end{cases}$

(e) Solve by method of separation of variables: $\frac{\partial u}{\partial t} = \frac{\partial u}{\partial x} - 2u$; $u(x,0) = 10e^{-x} - 6e^{-4x}$.

SECTION C

3. Attempt any *one* part of the following:

(a) Solve the simultaneous differential equations:

$$\frac{d^2x}{dt^2} - 4\frac{dx}{dt} + 4x = y \text{ and } \frac{d^2y}{dt^2} + 4\frac{dy}{dt} + 4y = 25x + 16e^t.$$

(b) Use variation of parameter method to solve the differential equation $x^2y'' + xy' - y = x^2e^x$.

4. Attempt any *one* part of the following:

(a) State and prove Rodrigue's formula for Legendre's polynomial.

(b) Solve in series: 2x(1-x)y'' + (1-x)y' + 3y = 0.

5. Attempt any *one* part of the following:

(a) State convolution theorem and hence find inverse Laplace transform of $\frac{s^2}{(s^2 + a^2)(s^2 + b^2)}$.

(b) Solve the following differential equation using Laplace transform $\frac{d^3y}{dt^3} - 3\frac{d^2y}{dt^2} + 3\frac{dy}{dt} - y = t^2e^t$ where y(0) = 1, y'(0) = 0 and y''(0) = -2.

6. Attempt any *one* part of the following:

(a)

(a)

Obtain Fourier series for the function
$$f(x) = \begin{cases} x, & -\pi < x \le 0 \\ -x, & 0 < x < \pi \end{cases}$$
 and hence show

$$\frac{1}{1^2} + \frac{1}{3^2} + \frac{1}{5^2} + \dots = \frac{\pi^2}{8}.$$

(b) Solve the linear partial differential equation: $\frac{\partial^2 z}{\partial x^2} - 2\frac{\partial^2 z}{\partial x \partial y} = \sin x \cos 2y$.

7. Attempt any *one* part of the following:

A string is stretched and fastened to two points *l* apart. Motion is started by displacing the string in the form $y = A \sin \frac{\pi x}{l}$ from which it is released at time t = 0. Find the displacement of any point at a distance x from any and at any time t

point at a distance x from one end at any time t.

(b) A rectangular plate with insulated surfaces is 8 cm wide and so long compared to its width that it may be considered infinite in length without introducing an appreciable error. If the temperature

along one short edge y = 0 is given by $u(x,0) = 100\sin\frac{\pi x}{8}, 0 < x < 8$

while the two long edges x = 0 and x = 8 as well as the other short edge are kept at $0^{\circ}C$. Find the temperature u(x, y) at any point in steady state.

 $7 \ge 1 = 7$

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that