

(Following Paper ID and Roll No. to be filled in your Answer Book)

Paper ID : 199111

Roll No.

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B.Tach.

(SEM. I) THEORY EXAMINATION, 2015-16

ENGINEERING MATHEMATICS-I

[Time : 3 hours]

[Total Marks : 100]

SECTION-A

1. Attempt all parts. All parts carry equal marks. Write answer of each part in shots. (10×2=20)

(a) If $u = \log(x^2/y)$ then value of $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} = ?$

(b) If $z = xyf(x/y)$ then value of $x \frac{\partial z}{\partial x} + y \frac{\partial z}{\partial y} = 2z$

(c) Apply Taylor's series find expansion of $f(x, y) = x^3 + xy^2$ about point (2, 1) upto first degree term.

(d) If $x = u - v, y = u^2 - v^2$, find the value of $\frac{\partial(u, v)}{\partial(x, y)}$.

(e) Find all the asymptotes of the curve $xy^2 = 4a^2(2a - x)$

- (f) Find the inverse of the matrix by using elementary row operation. $A = \begin{bmatrix} 1 & 2 \\ 5 & 7 \end{bmatrix}$

(g) If $A = \begin{bmatrix} -1 & 0 & 0 \\ 2 & -3 & 0 \\ 1 & 4 & -2 \end{bmatrix}$, find the eigen value of A^2

(h) Evaluate $\int_0^1 \int_1^2 \int_2^3 xyz \, dx \, dy \, dz$.

- (i) If $\phi(x, y, z) = x^2y + y^2x + z^2$, find $\nabla\phi$ at the point (1, 1, 1).

(j) Evaluate $\frac{r(8/3)}{r(2/3)}$.

SECTION-B

Attempt any five from this section.

(10x5=50)

2. If $x = \sin\left\{\frac{1}{m} \sin^{-1} y\right\}$ find the value of y_n at $x=0$
3. if u, v, w are the roots of the equation $(\lambda-x)^3 + (\lambda-y)^3 + (\lambda-z)^3 = 0$ in λ find $\frac{\partial(u, v, w)}{\partial(x, y, z)}$.

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(2)

AS-101

4. If r the distance of a point on conic $ax^2 + by^2 + cz^2 = 1$, $lx + my + nz = 0$ from origin, then that the stationary values of r are given by the equation

$$\frac{l^2}{1-ar^2} + \frac{m^2}{1-br^2} + \frac{n^2}{1-cr^2} = 0$$

5. Find the Eigen values and corresponding Eigen

vectors $A = \begin{bmatrix} 6 & -2 & 2 \\ -2 & 3 & -1 \\ 2 & -1 & 3 \end{bmatrix}$

6. The plane $\frac{x}{a} + \frac{y}{b} + \frac{z}{c} = 1$ meets the axes in A, B, and C.

Apply Dirichlet's integral to find the volume of the tetrahedron OABC. Also find its mass if the density at any point is $kxyz$.

7. Change the order of Integration in $I = \int_0^1 \int_{x^2}^{2-x} xy \, dx \, dy$ and hence evaluate the same.

8. Verify Gauss's divergence theorem for the function $\vec{F} = x^2\hat{i} + z\hat{j} + yz\hat{k}$, taken over the cube bounded by $x=0, x=1, y=0, y=1$ and $z=0, z=1$.

9. Show that the vector field $\vec{F} = \frac{\vec{r}}{|\vec{r}|^3}$ is irrotational as well as solenoidal. Find the scalar potential.

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SECTION-C

Attempt any **two** question from this section. (15x2=30)

10. (a) Expand $e^{ax} \cos by$ in power of in powers of x and y as terms of third degree.

(b) Determine the constant a and b such that the curl of vector.

$$\vec{A} = (2xy + 3yz)\hat{i} + (x^2 + axz - 4z^2)\hat{j} - (3xy + byz)\hat{k}$$

is zero.

(c) Examine the following vector for linearly dependent and find the relation between them. If Possible.

$$X_1 = (1, 1, -1, 1), X_2 = (1, 1, 2, -1), X_3 = (3, 1, 0, 1).$$

11. (a) Define Beta and Gamma function and Evaluate

$$\int_0^1 \frac{dx}{\sqrt{1+x^4}}.$$

(b) Find the area between the parabola $y^2 = 4ax$ and $x^2 = 4ay$.

(c) If $y_1 = \frac{x_2 x_3}{x_1}, y_2 = \frac{x_3 x_1}{x_2}, y_3 = \frac{x_1 x_2}{x_3}$ find $\frac{\partial(y_1, y_2, y_3)}{\partial(x_1, x_2, x_3)}$.

12. (a) Evaluate $\int_0^1 \frac{dx}{(a^n - x^n)^{1/n}}$.

(b) Reduce the matrix in to normal form and hence

$$\text{find its rank } \begin{bmatrix} 1 & 2 & 1 & 0 \\ -2 & 4 & 3 & 0 \\ 1 & 0 & 2 & -8 \end{bmatrix}$$

(c) It $u = u\left(\frac{y-x}{xy}, \frac{z-x}{xz}\right)$, show that :

$$x^2 \frac{\partial u}{\partial x} + y^2 \frac{\partial u}{\partial y} + z^2 \frac{\partial u}{\partial z} = 0.$$

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